# Sorting Algorithms

The 3 sorting methods discussed here all have wild signatures. For example,

public static <E extends Comparable<? super E>>void BubbleSort(E[] array )

The underlined portion is a *type bound*. This says that the generic type E used as the base type of the array must implement or extend a superclass that implements, the Comparable interface (which says that E has a compareTo(E) method. See the discussion in Weiss of wildcards and type bounds,p. 151-154.

In less generic examples you probably don't need this. If you are writing BubbleSort to sort strings its signature could just be public static void BubbleSort(String[] array)

### BubbleSort

BubbleSort makes repeated passes through the array, interchanging successive elements that are out of order. When no changes are made in a pass the array is sorted.

```
public static <E extends Comparable<? super E>>void BubbleSort(E[]
array){
        boolean sorted = false;
        int highest = array.length-1;
        while (!sorted) {
                sorted = true;
                 for (int i = 0; i < highest; i++) {
                         if (array[i].compareTo(array[i+1]) > 0) {
                                  E buffer = array[i];
                                  array[i] = array[i+1];
                                 array[i+1] = buffer;
                                 sorted = false;
                 highest -= 1;
```

#### Original data

33	12	45	17	23	52	24
					-	
12	33	17	23	45	24	52
12	17	23	33	24	45	52
12	17	23	24	33	45	52
12	17	23	24	33	45	52

Each row shows the result of a pass through the previous row, flipping consecutive elements that are out of order.

The first pass through the list does (n-1) comparisons. That pass puts the largest element into its proper location at the last spot in the list, so the next pass does (n-2) comparisons. Altogether we do at most

$$(n-1)+(n-2)+...+1 = n(n-1)/2$$

comparisons. For each comparison we do at most 1 interchange, which takes 3 assignment statements. This means BubbleSort is worst-case  $O(n^2)$ .

Note that the best case for BubbleSort is when the data is already sorted; only one pass is then needed and the running time is O(n). Of course, if you knew the data was already sorted there wouldn't be a lot of point in calling BubbleSort

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## SelectionSort

SelectionSort finds the smallest element and puts it at position 0, the smallest remaining element and puts it at position 1, etc.

```
public static <E extends Comparable<? super E>>void
                                           SelectionSort(E[] array ) {
        for (int i=0; i < array.length-1; i++) {
                 // find the index of the smallest remaining element
                 int small = i;
                 for (int j = i+1; j < array.length; j++) {
                         if (array[j].compareTo(array[small]) < 0)</pre>
                                  small = j;
                 // put the smallest remaining element at position i
                 E buffer = array[i];
                 array[i] = array[small];
                 array[small]= buffer;
```

#### Original data

		U				
33	12	45	17	23	52	24
12	33	45	17	23	52	24
12	17	45	33	23	52	24
12	17	23	33	45	52	24
12	17	23	24	45	52	33
12	17	23	24	33	52	45
12	17	23	24	33	45	52

The element put in its final location is in blue.

Selection sort does (n-1) passes. The first one does (n-1) comparisons; the second (n-2) comparisons, and so forth. There are a total of

$$(n-1) + (n-2) + (n-3) + ... + 1 = n(n-1)/2$$

comparisons. This is very similar to BubbleSort, only instead of interchanging elements of the array, which takes 3 assignments, here each comparison results in at most one integer assignment. Both are worst-case  $O(n^2)$ , but in specific examples SelectionSort usually runs somewhat faster.

Question: Suppose you use SelectionSort on an array of size n that is already sorted. How many comparisons will the sorting algorithm do?

- A. None
- B. 1
- C. O(n)
- D.  $O(n^2)$

Answer D:  $O(n^2)$ .

Unlike BubbleSort, SelectionSort doesn't have a quick way out if the data is already sorted; it always does n\*(n-1)/2 comparisons.

### InsertionSort

InsertionSort maintains a sorted portion of the array (the front) and inserts elements from the unsorted portion into it.

```
public static <E extends Comparable<? super E>>void
                                      InsertionSort(E[] array ) {
      for (int p = 1; p < array.length; p++) {
             // p is the start of the unsorted portion
          E item = array[p];
          int j;
          for (j=p; j > 0 \&\& item.compareTo(array[j-1]) < 0; j--)
               array[j] = array[j-1];
          array[j]= item;
```

#### Original data

		_				
33	12	45	17	23	52	24
12	33	45	17	23	52	24
12	33	45	17	23	52	24
12	17	33	45	23	52	24
12	17	23	33	45	52	24
12	17	23	33	45	52	24
12	17	23	24	33	45	52
12	17	25	24	33	45	52

The sorted portion of the array is in blue.

It is easy to see that InsertionSort is no worse than  $O(n^2)$  -- the outer loop runs n times, and the inner loop also takes at most n steps -- n steps done n times gives a total of  $n^2$  steps.

The worst case is when the data is reversesorted (biggest to smallest); the first pass does 1 comparison, the second 2, and so forth. Altogether this does 1+2+3+...+(n-1) = n(n-1)/2 comparisons.

Question: Suppose you use InsertionSort on an array of size n that is already sorted. How many comparisons will the sorting algorithm do?

- A. None
- B. 1
- C. O(n)
- D.  $O(n^2)$

Answer C: O(n)

If the data is already sorted, each pass does only one comparison and one assignment statement, so the algorithm runs in O(n) steps.

InsertionSort is a good choice if you have a small amount of data to sort; it tends to be faster than the other simple sorts and is easy to implement.

If you want to sort data the size of the NY phone book, InsertionSort is a terrible choice. There are sorting algorithms that are  $O(n^*log(n))$ , which is vastly better than  $O(n^2)$  when n is large.